

APPENDIX IIA

CHARACTER TABLES FOR CHEMICALLY IMPORTANT SYMMETRY GROUPS*

1. The Nonaxial Groups

C_1	E
A	1

C_2	E	σ_h		C_i	E	i			
A'	1	1	x, y, R_z	x^2, y^2, z^2, xy	A_g	1	1	R_x, R_y, R_z	$x^2, y^2, z^2, xy, xz, yz$
A''	1	-1	z, R_x, R_y	yz, xz	A_u	1	-1	x, y, z	

2. The C_n Groups

C_2	E	C_2	
A	1	1	z, R_z
B	1	-1	x, y, R_x, R_y

C_3	E	C_3	C_3^2		$\epsilon = \exp(2\pi i/3)$
A	1	1	1	z, R_z	$x^2 + y^2, z^2$
E	$\begin{Bmatrix} 1 & \epsilon & \epsilon^* \\ 1 & \epsilon^* & \epsilon \end{Bmatrix}$	$(x, y)(R_x, R_y)$	$(x^2 - y^2, xy)(yz, xz)$		

* Appendix IIA is presented in two places: (1) here, in its proper location in the sequence of appendices, and (2) as a separate section in a pocket inside the back cover.

The C_n Groups (continued)

C_4	E	C_4	C_2	C_4^3	
A	1	1	1	1	z, R_z
B	1	-1	1	-1	
E	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$	(x, y)			

C_5	E	C_5	C_5^2	C_5^3	C_5^4
A	1	1	1	1	1
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^{2*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^2 & \epsilon \end{Bmatrix}$				
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^* & \epsilon & \epsilon^{2*} \\ 1 & \epsilon^{2*} & \epsilon & \epsilon^* & \epsilon^2 \end{Bmatrix}$				

C_6	E	C_6	C_3	C_2
A	1	1	1	1
B	1	-1	1	-1
E_1	$\begin{Bmatrix} 1 & \epsilon & -\epsilon^* & -1 \\ 1 & \epsilon^* & -\epsilon & -1 \end{Bmatrix}$			
E_2	$\begin{Bmatrix} 1 & -\epsilon^* & -\epsilon & 1 \\ 1 & -\epsilon & -\epsilon^* & 1 \end{Bmatrix}$			

C_7	E	C_7	C_7^2	C_7^3	C_7^4
A	1	1	1	1	1
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^3 & \epsilon^{3*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^{3*} & \epsilon^3 & \epsilon \end{Bmatrix}$				
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^{3*} & \epsilon^* & \epsilon & \epsilon^{3*} \\ 1 & \epsilon^{2*} & \epsilon^3 & \epsilon & \epsilon^* & \epsilon^2 \end{Bmatrix}$				
E_3	$\begin{Bmatrix} 1 & \epsilon^3 & \epsilon^* & \epsilon^2 & \epsilon^2 & \epsilon^* \\ 1 & \epsilon^{3*} & \epsilon & \epsilon^{2*} & \epsilon^2 & \epsilon^* \end{Bmatrix}$				

C_8	E	C_8	C_4	C_2
A	1	1	1	1
B	1	-1	1	-1
E_1	$\begin{Bmatrix} 1 & \epsilon & i & -\epsilon^* & -1 \\ 1 & \epsilon^* & -i & -\epsilon & -1 \end{Bmatrix}$			
E_2	$\begin{Bmatrix} 1 & i & -1 & -i & 1 \\ 1 & -i & -1 & i & 1 \end{Bmatrix}$			
E_3	$\begin{Bmatrix} 1 & -\epsilon & i & \epsilon^* & -1 \\ 1 & -\epsilon^* & -i & \epsilon & -1 \end{Bmatrix}$			

The C_n Groups (continued)

C_4	E	C_4	C_2	C_4^3		
A	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1		$x^2 - y^2, xy$
E	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$				$(x, y)(R_x, R_y)$	(yz, xz)

C_5	E	C_5	C_5^2	C_5^3	C_5^4		$\epsilon = \exp(2\pi i/5)$
A	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^{2*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^2 & \epsilon \end{Bmatrix}$					$(x, y)(R_x, R_y)$	(yz, xz)
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^* & \epsilon & \epsilon^{2*} \\ 1 & \epsilon^{2*} & \epsilon & \epsilon^* & \epsilon^2 \end{Bmatrix}$						$(x^2 - y^2, xy)$

C_6	E	C_6	C_3	C_2	C_3^2	C_6^5		$\epsilon = \exp(2\pi i/6)$
A	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	1	-1		
E_1	$\begin{Bmatrix} 1 & \epsilon & -\epsilon^* & -1 & -\epsilon & \epsilon^* \\ 1 & \epsilon^* & -\epsilon & -1 & -\epsilon^* & \epsilon \end{Bmatrix}$						(x, y) (R_x, R_y)	(xz, yz)
E_2	$\begin{Bmatrix} 1 & -\epsilon^* & -\epsilon & 1 & -\epsilon^* & -\epsilon \\ 1 & -\epsilon & -\epsilon^* & 1 & -\epsilon & -\epsilon^* \end{Bmatrix}$							$(x^2 - y^2, xy)$

C_7	E	C_7	C_7^2	C_7^3	C_7^4	C_7^5	C_7^6		$\epsilon = \exp(2\pi i/7)$
A	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
E_1	$\begin{Bmatrix} 1 & \epsilon & \epsilon^2 & \epsilon^3 & \epsilon^{3*} & \epsilon^{2*} & \epsilon^* \\ 1 & \epsilon^* & \epsilon^{2*} & \epsilon^{3*} & \epsilon^3 & \epsilon^2 & \epsilon \end{Bmatrix}$							(x, y) (R_x, R_y)	(xz, yz)
E_2	$\begin{Bmatrix} 1 & \epsilon^2 & \epsilon^{3*} & \epsilon^* & \epsilon & \epsilon^3 & \epsilon^{2*} \\ 1 & \epsilon^{2*} & \epsilon^3 & \epsilon & \epsilon^* & \epsilon^{3*} & \epsilon^2 \end{Bmatrix}$								$(x^2 - y^2, xy)$
E_3	$\begin{Bmatrix} 1 & \epsilon^3 & \epsilon^* & \epsilon^2 & \epsilon^{2*} & \epsilon & \epsilon^{3*} \\ 1 & \epsilon^{3*} & \epsilon & \epsilon^{2*} & \epsilon^2 & \epsilon^* & \epsilon^3 \end{Bmatrix}$								

C_8	E	C_8	C_4	C_2^3	C_2	C_4^3	C_4^5	C_4^7		$\epsilon = \exp(2\pi i/8)$
A	1	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	1	-1	1	-1		
E_1	$\begin{Bmatrix} 1 & \epsilon & i & -\epsilon^* & -1 & -\epsilon & -i & \epsilon^* \\ 1 & \epsilon^* & -i & -\epsilon & -1 & -\epsilon^* & i & \epsilon \end{Bmatrix}$								(x, y) (R_x, R_y)	(xz, yz)
E_2	$\begin{Bmatrix} 1 & i & -1 & -i & 1 & i & -1 & -i \\ 1 & -i & -1 & i & 1 & -i & -1 & i \end{Bmatrix}$									$(x^2 - y^2, xy)$
E_3	$\begin{Bmatrix} 1 & -\epsilon & i & \epsilon^* & -1 & \epsilon & -i & -\epsilon^* \\ 1 & -\epsilon^* & -i & \epsilon & -1 & \epsilon^* & i & -\epsilon \end{Bmatrix}$									

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i		
1	R_x, R_y, R_z	x^2, y^2, z^2 xy, xz, yz
-1	x, y, z	

$\pi i/3$

 $y)(yz, xz)$

proper location in the sequence of
the back cover.

3. The D_n Groups

D_2	E	$C_2(z)$	$C_2(y)$	$C_2(x)$		
A_1	1	1	1	1		x^2, y^2, z^2
B_1	1	1	-1	-1	z, R_z	xy
B_2	1	-1	1	-1	y, R_y	xz
B_3	1	-1	-1	1	x, R_x	yz

D_3	E	$2C_3$	$3C_2$		
A_1	1	1	1		$x^2 + y^2, z^2$
A_2	1	1	-1	z, R_z	
E	2	-1	0	$(x, y)(R_x, R_y)$	$(x^2 - y^2, xy)(xz, yz)$

D_4	E	$2C_4$	$C_2(=C_4^2)$	$2C_2'$	$2C_2''$	
A_1	1	1	1	1	1	$x^2 + y^2, z^2$
A_2	1	1	1	-1	-1	z, R_z
B_1	1	-1	1	1	-1	$x^2 - y^2$
B_2	1	-1	1	-1	1	xy
E	2	0	-2	0	0	$(x, y)(R_x, R_y)$ (xz, yz)

D_5	E	$2C_5$	$2C_5^2$	$5C_2$	
A_1	1	1	1	1	$x^2 + y^2, z^2$
A_2	1	1	1	-1	z, R_z
E_1	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y)(R_x, R_y)$ (xz, yz)
E_2	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	$(x^2 - y^2, xy)$

D_6	E	$2C_6$	$2C_3$	C_2	$3C_2'$	$3C_2''$	
A_1	1	1	1	1	1	1	$x^2 + y^2, z^2$
A_2	1	1	1	1	-1	-1	z, R_z
B_1	1	-1	1	-1	1	-1	
B_2	1	-1	1	-1	-1	1	
E_1	2	1	-1	-2	0	0	$(x, y)(R_x, R_y)$ (xz, yz)
E_2	2	-1	-1	2	0	0	$(x^2 - y^2, xy)$

4. The C_{nv} Groups

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma'_v(yz)$
A_1	1	1	1	1
A_2	1	1	-1	-1
B_1	1	-1	1	-1
B_2	1	-1	-1	1

C_{3v}	E	$2C_3$	$3\sigma_v$	
A_1	1	1	1	z
A_2	1	1	-1	R_z
E	2	-1	0	(x, y)

C_{4v}	E	$2C_4$	C_2	$2\sigma_v$	$2\sigma_d$
A_1	1	1	1	1	1
A_2	1	1	1	-1	-1
B_1	1	-1	1	1	-1
B_2	1	-1	1	-1	1
E	2	0	-2	0	0

C_{5v}	E	$2C_5$	$2C_5^2$	$5C_2$
A_1	1	1	1	1
A_2	1	1	1	-1
E_1	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	$2 \cos 72^\circ$
E_2	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	$2 \cos 144^\circ$

C_{6v}	E	$2C_6$	$2C_3$	C_2	$3C_2'$	$3C_2''$
A_1	1	1	1	1	1	1
A_2	1	1	1	1	-1	-1
B_1	1	-1	1	-1	1	-1
B_2	1	-1	1	-1	-1	1
E_1	2	1	-1	-2	0	0
E_2	2	-1	-1	2	0	0

4. The C_{nv} Groups

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma'_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

C_{3v}	E	$2C_3$	$3\sigma_v$		
A_1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	-1	R_z	
E	2	-1	0	$(x, y)(R_x, R_y)$	$(x^2 - y^2, xy)(xz, yz)$

C_{4v}	E	$2C_4$	C_2	$2\sigma_v$	$2\sigma_d$		
A_1	1	1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	1	-1	-1	R_z	
B_1	1	-1	1	1	-1		$x^2 - y^2$
B_2	1	-1	1	-1	1		xy
E	2	0	-2	0	0	$(x, y)(R_x, R_y)$	(xz, yz)

C_{5v}	E	$2C_5$	$2C_5^2$	$5\sigma_v$		
A_1	1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	1	-1	R_z	
E_1	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y)(R_x, R_y)$	(xz, yz)
E_2	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$

C_{6v}	E	$2C_6$	$2C_3$	C_2	$3\sigma_v$	$3\sigma_d$		
A_1	1	1	1	1	1	1	z	$x^2 + y^2, z^2$
A_2	1	1	1	1	-1	-1	R_z	
B_1	1	-1	1	-1	1	-1		
B_2	1	-1	1	-1	-1	1		
E_1	2	1	-1	-2	0	0	$(x, y)(R_x, R_y)$	(xz, yz)
E_2	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

5. The C_{nh} Groups

C_{2h}	E	C_2	i	σ_h		
A_g	1	1	1	1	R_z	x^2, y^2, z^2, xy
B_g	1	-1	1	-1	R_x, R_y	xz, yz
A_u	1	1	-1	-1	z	
B_u	1	-1	-1	1	x, y	

C_{3h}	E	C_3	C_3^2	σ_h	S_3	S_3^5		$\varepsilon = \exp(2\pi i/3)$
A'	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E'	1	ε	ε^*	1	ε	ε^*	(x, y)	$(x^2 - y^2, xy)$
A''	1	1	1	-1	-1	-1	z	
E''	1	ε	ε^*	-1	$-\varepsilon$	$-\varepsilon^*$	(R_x, R_y)	(xz, yz)

C_{4h}	E	C_4	C_2	C_4^3	i	S_4^3	σ_h	S_4		
A_g	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B_g	1	-1	1	-1	1	-1	1	-1	(R_x, R_y)	$x^2 - y^2, xy$
E_g	1	i	-1	$-i$	1	i	-1	$-i$	z	
A_u	1	1	1	1	-1	-1	-1	-1		
B_u	1	-1	1	-1	-1	1	-1	1		
E_u	1	i	-1	$-i$	-1	$-i$	1	i	(x, y)	

C_{5h}	E	C_5	C_5^2	C_5^3	C_5^4	σ_h	S_5	S_5^7	S_5^3	S_5^9		$\varepsilon = \exp(2\pi i/5)$
A'	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E_1'	1	ε	ε^2	ε^{2*}	ε^*	1	ε	ε^2	ε^{2*}	ε^*	(x, y)	
E_2'	1	ε^2	ε^*	ε	ε^{2*}	1	ε^2	ε^*	ε	ε^{2*}		$(x^2 - y^2, xy)$
A''	1	1	1	1	1	-1	-1	-1	-1	-1	z	
E_1''	1	ε	ε^2	ε^{2*}	ε^*	-1	$-\varepsilon$	$-\varepsilon^2$	$-\varepsilon^{2*}$	$-\varepsilon^*$	(R_x, R_y)	(xz, yz)
E_2''	1	ε^2	ε^*	ε	ε^{2*}	-1	$-\varepsilon^2$	$-\varepsilon^*$	$-\varepsilon$	$-\varepsilon^{2*}$		

C_{6h}	E	C_6	C_3	C_2	C_3^2	C_6^5	i	S_3^5	S_6^5	σ_h	S_6	S_3		$\varepsilon = \exp(2\pi i/6)$
A_g	1	1	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B_g	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	(R_x, R_y)	(xz, yz)
E_{1g}	1	ε	ε^*	-1	$-\varepsilon$	ε^*	1	ε	$-\varepsilon^*$	-1	$-\varepsilon$	ε^*		
E_{2g}	1	ε^2	ε^*	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$		
A_u	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	z	$(x^2 - y^2, xy)$
B_u	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1		
E_{1u}	1	ε	ε^*	-1	$-\varepsilon$	ε^*	-1	$-\varepsilon$	ε^*	1	ε	$-\varepsilon^*$	(x, y)	
E_{2u}	1	ε^2	ε^*	1	$-\varepsilon^*$	$-\varepsilon$	-1	$-\varepsilon^*$	$-\varepsilon$	1	ε^*	$-\varepsilon$		

6. The D_{nh} Groups

D_{2h}	E	$C_2(z)$	$C_2(y)$	$C_2(x)$
A_g	1	1	1	1
B_{1g}	1	1	-1	-1
B_{2g}	1	-1	1	-1
B_{3g}	1	-1	-1	1
A_u	1	1	1	-1
B_{1u}	1	1	-1	-1
B_{2u}	1	-1	1	-1
B_{3u}	1	-1	-1	1

D_{3h}	E	$2C_3$	$3C_2$	σ_h	2
A_1'	1	1	1	1	
A_2'	1	1	-1	1	
E'	2	-1	0	2	-
A_1''	1	1	1	-1	-
A_2''	1	1	-1	-1	-
E''	2	-1	0	-2	-

D_{4h}	E	$2C_4$	C_2	$2C_2'$	$2C$
A_{1g}	1	1	1	1	
A_{2g}	1	1	1	-1	-
B_{1g}	1	-1	1	1	-
B_{2g}	1	-1	1	-1	-
E_g	2	0	-2	0	-
A_{1u}	1	1	1	1	
A_{2u}	1	1	1	-1	-
B_{1u}	1	-1	1	1	-
B_{2u}	1	-1	1	-1	-
E_u	2	0	-2	0	-

D_{5h}	E	$2C_5$	$2C_5^2$
A_1'	1	1	1
A_2'	1	1	1
E_1'	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$
E_2'	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$
A_1''	1	1	1
A_2''	1	1	1
E_1''	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$
E_2''	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$

D_{6h}	E	$2C_6$	$2C_3$	C_2	$3C_2$
A_{1g}	1	1	1	1	1
A_{2g}	1	1	1	1	-1
B_{1g}	1	-1	1	-1	1
B_{2g}	1	-1	1	-1	-1
E_{1g}	2	1	-1	-2	0
E_{2g}	2	-1	1	2	0
A_{1u}	1	1	1	1	1
A_{2u}	1	1	1	1	-1
B_{1u}	1	-1	1	-1	1
B_{2u}	1	-1	1	-1	-1
E_{1u}	2	1	-1	-2	0
E_{2u}	2	-1	1	2	0

6. The D_{nh} Groups

$= \exp(2\pi i/3)$

$x^2 + y^2, z^2$
 $x^2 - y^2, xy$

(x, y, z)

R_z	$x^2 + y^2, z^2$
	$x^2 - y^2, xy$
(xz, yz)	

S_5^0	$\varepsilon = \exp(2\pi i/5)$
1	R_z
ε^*	(x, y)
ε	
ε^{2*}	
ε^2	$(x^2 - y^2, xy)$
-1	z
$-\varepsilon^*$	(R_x, R_y)
$-\varepsilon$	(xz, yz)
$-\varepsilon^{2*}$	
$-\varepsilon^2$	

S_6	S_3	$\varepsilon = \exp(2\pi i/6)$
1	1	R_z
1	-1	
-1	ε^*	(R_x, R_y)
1	ε	(xz, yz)
1	$-\varepsilon^*$	
1	$-\varepsilon$	$(x^2 - y^2, xy)$
1	-1	z
1	1	
1	ε	(x, y)
1	$-\varepsilon^*$	
1	ε^*	
1	ε	

D_{2h}	E	$C_2(z)$	$C_2(y)$	$C_2(x)$	i	$\sigma(xy)$	$\sigma(xz)$	$\sigma(yz)$		
A_g	1	1	1	1	1	1	1	1		x^2, y^2, z^2
B_{1g}	1	1	-1	-1	1	1	-1	-1	R_z	xy
B_{2g}	1	-1	1	-1	1	-1	1	-1	R_y	xz
B_{3g}	1	-1	-1	1	1	-1	-1	1	R_x	yz
A_u	1	1	1	1	-1	-1	-1	-1		
B_{1u}	1	1	-1	-1	-1	-1	1	1		z
B_{2u}	1	-1	1	-1	-1	1	-1	1		y
B_{3u}	1	-1	-1	1	-1	1	1	-1		x

D_{3h}	E	$2C_3$	$3C_2$	σ_h	$2S_6$	$3\sigma_v$		
A_1'	1	1	1	1	1	1		$x^2 + y^2, z^2$
A_2'	1	1	-1	1	1	-1	R_z	
E_1'	2	-1	0	2	-1	0	(x, y)	$(x^2 - y^2, xy)$
A_1''	1	1	1	-1	-1	-1		
A_2''	1	1	-1	-1	-1	1	z	
E_2''	2	-1	0	-2	1	0	(R_x, R_y)	(xz, yz)

D_{4h}	E	$2C_4$	C_2	$2C_2'$	$2C_2''$	i	$2S_4$	σ_h	$2\sigma_v$	$2\sigma_d$	
A_{1g}	1	1	1	1	1	1	1	1	1	1	R_z
A_{2g}	1	1	1	-1	-1	1	1	1	-1	-1	
B_{1g}	1	-1	1	1	-1	1	-1	1	1	-1	
B_{2g}	1	-1	1	-1	1	1	-1	1	-1	1	
E_g	2	0	-2	0	0	2	0	-2	0	0	(R_x, R_y)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1	
A_{2u}	1	1	1	-1	-1	-1	-1	-1	1	1	z
B_{1u}	1	-1	1	1	-1	-1	1	-1	-1	1	
B_{2u}	1	-1	1	-1	1	-1	1	-1	1	-1	
E_u	2	0	-2	0	0	-2	0	2	0	0	(x, y)

D_{5h}	E	$2C_5$	$2C_5^2$	$5C_2$	σ_h	$2S_5$	$2S_5^3$	$5\sigma_v$	
A_1'	1	1	1	1	1	1	1	1	R_z
A_2'	1	1	1	-1	1	1	1	-1	
E_1'	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	(x, y)
E_2'	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	
A_1''	1	1	1	1	-1	-1	-1	-1	
A_2''	1	1	1	-1	-1	-1	-1	1	z
E_1''	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0	(R_x, R_y)
E_2''	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0	(xz, yz)

D_{6h}	E	$2C_6$	$2C_3$	C_2	$3C_2'$	$3C_2''$	i	$2S_6$	$2S_6^5$	σ_h	$3\sigma_d$	$3\sigma_v$	
A_{1g}	1	1	1	1	1	1	1	1	1	1	1	1	R_z
A_{2g}	1	1	1	1	-1	-1	1	1	1	1	-1	-1	
B_{1g}	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	
B_{2g}	1	-1	1	-1	-1	1	1	-1	1	-1	-1	1	
E_{1g}	2	1	-1	-2	0	0	2	1	-1	-2	0	0	(R_x, R_y)
E_{2g}	2	-1	1	2	0	0	2	-1	1	2	0	0	(xz, yz)
A_{1u}	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	z
A_{2u}	1	1	1	1	-1	-1	-1	-1	-1	-1	1	1	
B_{1u}	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1	
B_{2u}	1	-1	1	-1	-1	1	-1	1	-1	1	1	-1	
E_{1u}	2	1	-1	-2	0	0	-2	-1	1	2	0	0	(x, y)
E_{2u}	2	-1	1	2	0	0	-2	1	-1	-2	0	0	

6. The D_{nh} Groups (Continued).

D_{8h}	E	$2C_8$	$2C_8^3$	$2C_4$	C_2	$4C_2'$	$4C_2''$	i	$2S_8$	$2S_8^3$	$2S_4$	σ_h	$4\sigma_d$	$4\sigma_v$		
A_{1g}	1	1	1	1	1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	1	1	1	-1	-1	1	1	1	1	1	-1	-1		
B_{1g}	1	-1	-1	1	1	1	-1	1	-1	-1	1	1	1	-1		
B_{2g}	1	-1	-1	1	1	-1	1	1	-1	-1	1	1	-1	1		
E_{1g}	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	0	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	(R_x, R_y)	(xz, yz) $(x^2 - y^2, xy)$
E_{2g}	2	0	0	-2	2	0	0	2	0	0	-2	2	0	0		
E_{3g}	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0		
A_{1u}	1	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1		
A_{2u}	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	-1	-1	z	
B_{1u}	1	-1	-1	1	1	1	-1	-1	1	1	-1	-1	-1	-1		
B_{2u}	1	-1	-1	1	1	-1	1	-1	1	1	-1	-1	-1	-1		
E_{1u}	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	-2	$-\sqrt{2}$	$\sqrt{2}$	0	2	0	0		
E_{2u}	2	0	0	-2	2	0	0	2	0	0	2	-2	0	0		
E_{3u}	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	-2	$\sqrt{2}$	$-\sqrt{2}$	0	2	0	0		

7. The D_{nd} Groups

D_{2d}	E	$2S_4$	C_2	$2C_2'$	$2\sigma_d$				
A_1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$		
A_2	1	1	1	-1	-1				
B_1	1	-1	1	1	-1			z	$x^2 - y^2$
B_2	1	-1	1	-1	1				
E	2	0	-2	0	0	$(x, y);$ (R_x, R_y)	xy (xz, yz)		

D_{3d}	E	$2C_3$	$3C_2$	i	$2S_6$	$3\sigma_d$		
A_{1g}	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	-1	1	1	-1		
E_g	2	-1	0	2	-1	0		
A_{1u}	1	1	1	-1	-1	-1	z	(x, y)
A_{2u}	1	1	-1	-1	-1	1		
E_u	2	-1	0	-2	1	0		

D_{4d}	E	$2S_8$	$2C_4$	$2S_8^3$	C_2	$4C_2'$	$4\sigma_d$				
A_1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$		
A_2	1	1	1	1	1	-1	-1				
B_1	1	-1	1	-1	1	1	-1			z	$(x^2 - y^2, xy)$
B_2	1	-1	1	-1	1	-1	1				
E_1	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0	(R_x, R_y)	(xz, yz)		
E_2	2	0	-2	0	2	0	0				
E_3	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0				

D_{5d}	E	$2C_5$	$2C_5^2$	$5C_2$	i	$2S_{10}^3$	$2S_{10}$	$5\sigma_d$		
A_{1g}	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
A_{2g}	1	1	1	-1	-1	1	1	-1		
E_{1g}	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0		
E_{2g}	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		
A_{1u}	1	1	1	1	-1	-1	-1	-1	z	(x, y)
A_{2u}	1	1	1	-1	-1	-1	-1	1		
E_{1u}	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0		
E_{2u}	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0		

7. The D_{nd} Groups (Continued)

D_{6d}	E	$2S_{12}$	$2C_6$	$2S_4$	$2C_2$
A_1	1	1	1	1	1
A_2	1	1	1	1	1
B_1	1	-1	1	-1	1
B_2	1	-1	1	-1	1
E_1	2	$\sqrt{3}$	1	0	-1
E_2	2	1	-1	-2	-1
E_3	2	0	-2	0	2
E_4	2	-1	-1	2	-1
E_5	2	$-\sqrt{3}$	1	0	-1

8. The S_n Groups

S_4	E	S_4	C_2	S_4^3	
A	1	1	1	1	R
B	1	-1	1	-1	z
E	$\begin{pmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{pmatrix}$				$($

S_6	E	C_3	C_3^2	i	S_6^5
A_g	1	1	1	1	1
E_g	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & 1 & \epsilon \\ 1 & \epsilon^* & \epsilon & 1 & \epsilon^* \end{pmatrix}$				
A_u	1	1	1	-1	-1
E_u	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & -1 & -\epsilon \\ 1 & \epsilon^* & \epsilon & -1 & -\epsilon^* \end{pmatrix}$				

S_8	E	S_8	C_4	S_8^3	C
A	1	1	1	1	
B	1	-1	1	-1	
E_1	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & -\epsilon^* & - \\ 1 & \epsilon^* & -i & -\epsilon & - \end{pmatrix}$				
E_2	$\begin{pmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{pmatrix}$				
E_3	$\begin{pmatrix} 1 & -\epsilon^* & -i & \epsilon & - \\ 1 & -\epsilon & i & \epsilon^* & - \end{pmatrix}$				

9. The Cubic Groups

T	E	$4C_3$	$4C_3^2$	$3C_2$	
A	1	1	1	1	
E	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & 1 \\ 1 & \epsilon^* & \epsilon & 1 \end{pmatrix}$				
T	3	0	0	-1	(R_x)

7. The D_{nd} Groups (Continued).

σ_h	$4\sigma_d$	$4\sigma_v$		
1	1	1	R_z	$x^2 + y^2, z^2$
1	-1	-1		
1	1	-1		
1	-1	1		
-2	0	0	(R_x, R_y)	(xz, yz) $(x^2 - y^2, xy)$
2	0	0		
-2	0	0	z	
-1	-1	-1		
-1	1	1		
-1	-1	1		
-1	1	-1	(x, y)	
2	0	0		
-2	0	0		
2	0	0		

D_{6d}	E	$2S_{12}$	$2C_6$	$2S_4$	$2C_3$	$2S_{12}^5$	C_2	$6C_2'$	$6\sigma_d$			
A_1	1	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$	
A_2	1	1	1	1	1	1	1	-1	-1			
B_1	1	-1	1	-1	1	-1	1	1	-1			
B_2	1	-1	1	-1	1	-1	1	-1	1			z
E_1	2	$\sqrt{3}$	1	0	-1	$-\sqrt{3}$	-2	0	0	(R_x, R_y)	(x, y)	
E_2	2	1	-1	-2	-1	1	2	0	0			$(x^2 - y^2, xy)$
E_3	2	0	-2	0	2	0	-2	0	0			
E_4	2	-1	-1	2	-1	-1	2	0	0			
E_5	2	$-\sqrt{3}$	1	0	-1	$\sqrt{3}$	-2	0	0		(xz, yz)	

8. The S_n Groups

S_4	E	S_4	C_2	S_4^3		
A	1	1	1	1	R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	z	$x^2 - y^2, xy$
E	$\begin{pmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{pmatrix}$				$(x, y); (R_x, R_y)$	(xz, yz)

S_6	E	C_3	C_3^2	i	S_6^5	S_6		$\epsilon = \exp(2\pi i/3)$
A_g	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
E_g	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & 1 & \epsilon & \epsilon^* \\ 1 & \epsilon^* & \epsilon & 1 & \epsilon^* & \epsilon \end{pmatrix}$						(R_x, R_y)	$(x^2 - y^2, xy);$ (xz, yz)
A_u	1	1	1	-1	-1	-1	z	
E_u	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & -1 & -\epsilon & -\epsilon^* \\ 1 & \epsilon^* & \epsilon & -1 & -\epsilon^* & -\epsilon \end{pmatrix}$						(x, y)	

S_8	E	S_8	C_4	S_8^3	C_2	S_8^5	C_4^3	S_8^7		$\epsilon = \exp(2\pi i/8)$
A	1	1	1	1	1	1	1	1	R_z	$x^2 + y^2, z^2$
B	1	-1	1	-1	1	-1	1	-1	z	
E_1	$\begin{pmatrix} 1 & \epsilon & i & -\epsilon^* & -1 & -\epsilon & -i & \epsilon^* \\ 1 & \epsilon^* & -i & -\epsilon & -1 & -\epsilon^* & i & \epsilon \end{pmatrix}$								$(x, y);$ (R_x, R_y)	
E_2	$\begin{pmatrix} 1 & i & -1 & -i & 1 & i & -1 & -i \\ 1 & -i & -1 & i & 1 & -i & -1 & i \end{pmatrix}$									$(x^2 - y^2, xy)$
E_3	$\begin{pmatrix} 1 & -\epsilon^* & -i & \epsilon & -1 & \epsilon^* & i & -\epsilon \\ 1 & -\epsilon & i & \epsilon^* & -1 & \epsilon & -i & -\epsilon^* \end{pmatrix}$									(xz, yz)

9. The Cubic Groups

T	E	$4C_3$	$4C_3^2$	$3C_2$		$\epsilon = \exp(2\pi i/3)$
A	1	1	1	1		$x^2 + y^2 + z^2$
E	$\begin{pmatrix} 1 & \epsilon & \epsilon^* & 1 \\ 1 & \epsilon^* & \epsilon & 1 \end{pmatrix}$					$(2z^2 - x^2 - y^2,$ $x^2 - y^2)$
T	3	0	0	-1	$(R_x, R_y, R_z); (x, y, z)$	(xy, xz, yz)

$x^2 + y^2, z^2$
 $(x^2 - y^2, xy)$
 $x^2 + y^2, z^2$
 $(x^2 - y^2, xy)$
 (xz, yz)

S_{10}	$5\sigma_d$			
1	1	R_z	$x^2 + y^2, z^2$	
1	-1			
$\angle 144^\circ$	0		(R_x, R_y)	(xz, yz)
$\angle 72^\circ$	0			$(x^2 - y^2, xy)$
1	-1	z		
1	1			
$\angle 144^\circ$	0		(x, y)	
$\angle 72^\circ$	0			

9. The Cubic Groups (Continued).

T_h	E	$4C_3$	$4C_2$	$3C_2$	i	$4S_6$	$4S_6^5$	$3\sigma_h$		$\varepsilon = \exp(2\pi i/3)$
A_1	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
E_g	1	ε	ε^2	1	1	ε	ε^2	1	(R_1, R_2, R_3)	$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_d	1	ε^2	ε	1	1	ε^2	ε	1		(xz, yz, xy)
A_u	1	1	1	1	-1	-1	-1	-1		
E_u	1	ε	ε^2	1	-1	$-\varepsilon$	$-\varepsilon^2$	-1	(x, y, z)	
T_u	1	ε^2	ε	1	-1	$-\varepsilon^2$	$-\varepsilon$	-1		

T_d	E	$8C_3$	$3C_2$	$6S_4$	$6\sigma_d$	
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_1	3	0	-1	1	-1	(R_1, R_2, R_3)
T_2	3	0	-1	-1	1	(x, y, z)

O	E	$8C_3$	$3C_2 (= C_4^2)$	$6C_4$	$6C_2$	
A_1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_2	1	1	1	-1	-1	
E	2	-1	2	0	0	$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_1	3	0	-1	1	-1	$(R_1, R_2, R_3), (x, y, z)$
T_2	3	0	-1	-1	1	(xy, xz, yz)

O_h	E	$8C_3$	$6C_2$	$6C_4$	$3C_2 (= C_4^2)$	i	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$	
A_{1g}	1	1	1	1	1	1	1	1	1	1	$x^2 + y^2 + z^2$
A_{2g}	1	1	-1	-1	1	1	-1	1	1	-1	
E_g	2	-1	0	0	2	2	0	-1	2	0	$(2z^2 - x^2 - y^2, x^2 - y^2)$
T_{1g}	3	0	-1	1	-1	3	1	0	-1	-1	(R_1, R_2, R_3)
T_{2g}	3	0	1	-1	-1	3	-1	0	-1	1	(xz, yz, xy)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1	
A_{2u}	1	1	-1	-1	1	-1	1	-1	-1	1	
E_u	2	-1	0	0	2	-2	0	1	-2	0	
T_{1u}	3	0	-1	1	-1	-3	-1	0	1	1	(x, y, z)
T_{2u}	3	0	1	-1	-1	-3	1	0	1	-1	

10. The Groups $C_{\infty v}$ and $C_{\infty h}$

$C_{\infty v}$	E	$2C_{\infty^\phi}$
$A_1 \equiv \Sigma^+$	1	1
$A_2 \equiv \Sigma^-$	1	1
$E_1 \equiv \Pi$	2	$2 \cos \Phi$
$E_2 \equiv \Delta$	2	$2 \cos 2\Phi$
$E_3 \equiv \Phi$	2	$2 \cos 3\Phi$
...

$D_{\infty h}$	E	$2C_{\infty^\phi}$...
Σ_g^+	1	1	...
Σ_g^-	1	1	...
Π_g	2	$2 \cos \Phi$...
Δ_g	2	$2 \cos 2\Phi$...
...
Σ_u^+	1	1	...
Σ_u^-	1	1	...
Π_u	2	$2 \cos \Phi$...
Δ_u	2	$2 \cos 2\Phi$...
...

10. The Groups $C_{\infty v}$ and $D_{\infty h}$ for Linear Molecules

$\iota = \exp(2\pi i/3)$

	$x^2 + y^2 + z^2$
	$(2z^2 - x^2 - y^2, x^2 - y^2)$
(x, R_x, R_y, R_z)	(xz, yz, xy)
(y, z)	

$C_{\infty v}$	E	$2C_{\infty}^{\phi}$	\dots	$\infty\sigma_v$		
$A_1 \equiv \Sigma^+$	1	1	\dots	1	z	$x^2 + y^2, z^2$
$A_2 \equiv \Sigma^-$	1	1	\dots	-1	R_x	
$E_1 \equiv \Pi$	2	$2 \cos \Phi$	\dots	0	$(x, y); (R_x, R_y)$	(xz, yz)
$E_2 \equiv \Delta$	2	$2 \cos 2\Phi$	\dots	0		$(x^2 - y^2, xy)$
$E_3 \equiv \Phi$	2	$2 \cos 3\Phi$	\dots	0		
\dots	\dots	\dots	\dots	\dots		

$+ z^2$	
$x^2 - y^2, x^2 - y^2$	
$yz)$	

$D_{\infty h}$	E	$2C_{\infty}^{\phi}$	\dots	$\infty\sigma_v$	i	$2S_{\infty}^{\phi}$	\dots	∞C_2	
Σ_g^+	1	1	\dots	1	1	1	\dots	1	$x^2 + y^2, z^2$
Σ_g^-	1	1	\dots	-1	1	1	\dots	-1	R_x
Π_g	2	$2 \cos \Phi$	\dots	0	2	$-2 \cos \Phi$	\dots	0	(R_x, R_y)
Δ_g	2	$2 \cos 2\Phi$	\dots	0	2	$2 \cos 2\Phi$	\dots	0	(xz, yz)
\dots	\dots	\dots	\dots	\dots	\dots	\dots	\dots	\dots	$(x^2 - y^2, xy)$
Σ_u^+	1	1	\dots	1	-1	-1	\dots	-1	z
Σ_u^-	1	1	\dots	-1	-1	-1	\dots	1	
Π_u	2	$2 \cos \Phi$	\dots	0	-2	$2 \cos \Phi$	\dots	0	(x, y)
Δ_u	2	$2 \cos 2\Phi$	\dots	0	-2	$-2 \cos 2\Phi$	\dots	0	
\dots	\dots	\dots	\dots	\dots	\dots	\dots	\dots	\dots	

	$x^2 + y^2 + z^2$
	$(2z^2 - x^2 - y^2, x^2 - y^2)$
(x, z)	(xy, xz, yz)

$6\sigma_d$		
1	1	$x^2 + y^2 + z^2$
1	-1	
2	0	$(2z^2 - x^2 - y^2, x^2 - y^2)$
1	-1	(R_x, R_y, R_z)
1	1	(xz, yz, xy)
1	-1	
1	1	
2	0	
1	1	(x, y, z)
1	-1	

11. The Icosahedral Groups*

I_h	E	$12C_5$	$12C_5^2$	$20C_3$	$15C_2$	i	$12S_{10}$	$12S_{10}^3$	$20S_6$	15σ	
A_g	1	1	1	1	1	1	1	1	1	1	$x^2 + y^2 + z^2$
T_{1g}	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	(R_x, R_y, R_z)
T_{2g}	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	
G_g	4	-1	-1	1	0	4	-1	-1	1	0	$(2x^2 - y^2 - z^2, x^2 - y^2, xy, yz, zx)$
H_g	5	0	0	-1	1	5	0	0	-1	1	
A_u	1	1	1	1	1	-1	-1	-1	-1	-1	
T_{1u}	3	$\frac{1}{2}(1 + \sqrt{5})$	$\frac{1}{2}(1 - \sqrt{5})$	0	-1	-3	$-\frac{1}{2}(1 - \sqrt{5})$	$-\frac{1}{2}(1 + \sqrt{5})$	0	1	(x, y, z)
T_{2u}	3	$\frac{1}{2}(1 - \sqrt{5})$	$\frac{1}{2}(1 + \sqrt{5})$	0	-1	-3	$-\frac{1}{2}(1 + \sqrt{5})$	$-\frac{1}{2}(1 - \sqrt{5})$	0	1	
G_u	4	-1	-1	1	0	-4	1	1	-1	0	
H_u	5	0	0	-1	1	-5	0	0	-1	-1	

*For the pure rotation group I , the outlined section in the upper left is the character table; the g subscripts should, of course, be dropped and (x, y, z) assigned to the T_1 representation

APPENDIX II

CORRELATION GROUP O_h

This table shows how the rep. posed into those of its subg. This table covers only representations of complexes. A will be found as Table X-1. J. C. Decius, and P. C. Cro

O_h	O	T_d	D_{4h}	D_{2d}
A_{1g}	A_1	A_1	A_{1g}	A_1
A_{2g}	A_2	A_2	B_{1g}	B_1
E_g	E	E	$A_{1g} + B_{1g}$	$A_1 + B$
T_{1g}	T_1	T_1	$A_{2g} + E_g$	$A_2 + E$
T_{2g}	T_2	T_2	$B_{2g} + E_g$	$B_2 + E$
A_{1u}	A_1	A_2	A_{1u}	B_1
A_{2u}	A_2	A_1	B_{1u}	A_1
E_u	E	E	$A_{1u} + B_{1u}$	$A_1 + E$
T_{1u}	T_1	T_2	$A_{2u} + E_u$	$B_2 + E$
T_{2u}	T_2	T_1	$B_{2u} + E_u$	$A_2 + E$